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## **KIRIRI WOMEN'S UNIVERSITY OF SCIENCE AND TECHNOLOGY UNIVERSITY EXAMINATION, 2024/2025 ACADEMIC YEAR** FIRST YEAR, FIRST SEMESTER EXAMINATION FOR THE BACHELOR OF BUSINESS AND INFORMATION TECHNOLOGY **KMA 2103 – BASIC MATHEMATICS**

Date: 04<sup>TH</sup> December 2024 Time: 11:30AM - 1:30PM

### **INSTRUCTIONS TO CANDIDATES** ANSWER QUESTION ONE (COMPULSORY) AND ANY OTHER TWO QUESTIONS **QUESTION ONE (30 MARKS)**

Solve without using tables or a calculator a)

# $log_{10}75 + log_{10}9 + log_{10}5$

 $log_{10}5 + log_{10}45$ 

|  |   |  | (3 Marks)       |  |
|--|---|--|-----------------|--|
| b)   | A group of young men decided to raise <i>Ksh</i> . <b>480</b> , <b>000</b> to start a business. Before the actual payment |  |                 |  |
|  |   | le, four members pulled out and each of those remaining had to pay an additional |                 |  |
|  |   | <b>0,000</b> . Determine the original number of members.                         | (4 Marks)       |  |
| c)   |   | $0 \times 39 \times 38 \times 37$ in factorial notation.                         | (1 Mark)        |  |
| d)   | Write down the coefficients of the terms indicated in the expansion of the following;                                     |  |                 |  |
|  | . ,   | $(1+x)^{16}$ , 3 <sup>rd</sup> term  | (3 Marks)       |  |
|  | . ,   | $(2-x)^{20}$ , 18 <sup>th</sup> term   | (3 Marks)       |  |
| e)   | Find how many different arrangements of 11 letters can be obtained from the letters                                       |  | s of the word   |  |
|  | MISSIS  | SIPPI  | (3 Marks)       |  |
| f)   | A polynomial $f(x)$ has remainder 9 when divided by $(x - 3)$ and remainder -5 when divided by 2                          |  | vided by $2x +$ |  |
|  |   | the remainder when divided by $(x - 3)(2x + 1)$                                  | (3 Marks)       |  |
| g) In an arithmetic progression the $4^{th}$ term is 13 and the $7^{th}$ term is 22. Find; |   |  |                 |  |
|  | i)  | The first term and the common difference   | (2 Marks)       |  |
|  | ii)   | The value of $n$ if the $n^{th}$ term is 100                                     | (2 Marks)       |  |
|  | iii)  | The value of m if the sum of m terms of the series is 175.                       |                 |  |
|  |   |  | (3 Marks)       |  |
| h)   | The roots of the equation $5x^2 + 12x + 6 = 0$ are $\alpha$ and $\beta$ . Find the equation of the integral coefficient   |  | al coefficients |  |
|  | whose re  | bots are $(\alpha - 1)$ and $(\beta - 1)$ .                                      | (3 Marks)       |  |

#### **QUESTION TWO (20 MARKS)**

a) Simplify 
$$\frac{\frac{1}{2}x^2(1+x)^{-\frac{1}{2}}-\frac{1}{2}x^{-\frac{1}{2}}(1+x)^{\frac{1}{2}}}{x}$$
 (4 Marks)

Use Complete the square method to solve for x in the function  $x^2 + x + 1 = 0$ b)

(4 Marks)

| c) | If $0 < x < \prod$ and $tan(X - A) = 3$ , where $tan A = 2$ , show that $x = \frac{3}{4} \prod$ without using tables |           |
|----|--|-----------|
|    |  | (4 Marks) |

d) Find the first four terms in the expansion of  $\sqrt{1-8x}$  in ascending power of x. Hence, substitute x = 0.01 and obtain the value of 23 correct to four significant figures (8 Marks)

#### **QUESTION THREE (20 MARKS)**

| a) | Solve for x given $log_2 1 + log_4 \frac{1}{2} = log_9 x$ | (4 Marks) |
|----|---|-----------|
|    |   |           |

b) Show that the solution of the general quadratic equation  $ax^2 + bx + c = 0$  is given by  $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ Hence solve the equation  $x^2 + 15x + 56 = 0$ . (7 Marks)

- c) Find the general solution of the equation  $\cos 2x 3\cos x + 2 = 0$  (7 Marks)
- d) State the quotient and the remainder when  $9x^3 5x + 5$  is divided by 2x 5

(2 Marks)

#### **QUESTION FOUR (20 MARKS)**

| a) | Show that $tan(A - B) = \frac{tan A - tan B}{1 + tan A tan B}$                      | (6 Marks) |
|----|---|-----------|
| b) | How many even numbers greater than 50000 can be formed using the digits 0,3,4,5,6,7 |           |
|    | i) without repetitions  | (6 Marks) |
|    | ii) if repetitions are allowed  | (4 Marks) |
| c) | Simplify without using tables or calculator;  |           |

$$4\cos 30^{\circ}\sin 27.59^{\circ} - 4\sin 45^{\circ}\cos 62.41^{\circ} - 16\tan 45^{\circ}\sin 60^{\circ}$$
 (4 Marks)

#### **QUESTION FIVE (20 MARKS)**

a) Simplify 
$$\frac{\sqrt{xy} \times x^{\frac{1}{3}} \times 2y^{\frac{1}{4}}}{(x^{10}y^9)^{\frac{1}{12}}}$$
 (3 Marks)

- b) The first term of an arithmetic progression is -12, and the last term is 40. If the sum of the progression is 196, find the number of terms and the common difference. (5 Marks)
- c) *Ksh.* 100,000 was invested on 1<sup>st</sup> January 1990. An additional of *Ksh.* 6,000 was added to the investment at the beginning of each subsequent year. The investment earns a compound interest of 8% per annum. Find the value of the investment on 31<sup>st</sup> December 2000. (7 Marks)
- d) Find the first four terms in the expansion of  $(1 8x)^{\frac{1}{3}}$  in ascending powers of x. Hence, substitute  $x = \frac{1}{100}$  and obtain the value of  $\sqrt[3]{23}$  correct to 5 significant figures (5 Marks)