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KIRIRI WOMENS' UNIVERSITY OF SCIENCE AND TECHNOLOGY UNIVERSITY EXAMINATIONS, 2024/2025 ACADEMIC YEAR FIRST YEAR, FIRST SEMESTER EXAMINATION FOR THE DEGREE OF BACHELOR OF SCIENCE (COMPUTER SCIENCE)

KMA 2100: FOUNDATION MATHEMATICS

Date: 4TH DECEMBER, 2024

Time: 11:30AM-1:30PM

INSTRUCTIONS TO CANDIDATES

ANSWER QUESTION ONE (COMPULSORY) AND ANY OTHER TWO QUESTIONS

QUESTION ONE: COMPULSORY (30 MARKS)

a) Solve without using tables or a calculator

$$\frac{log_{10}75 + log_{10}9 + log_{10}5}{log_{10}5 + log_{10}45}$$

(3 Marks)

- b) A group of young men decided to raise *Ksh*. **480,000** to start a business. Before the actual payment was made, four members pulled out and each of those remaining had to pay an additional *Ksh*. **20,000**. Determine the original number of members. (4 Marks)
- c) Write $40 \times 39 \times 38 \times 37$ in factorial notation.

(1 Mark)

- d) Write down the coefficients of the terms indicated in the expansion of the following:
 - (i) $(1 + x)^{16}$, 3rd term

(3 Marks)

(ii) $(2-x)^{20}$, 18th term

(3 Marks)

- e) Find how many different arrangements of 11 letters can be obtained from the letters of the word MISSISSIPPI (3 Marks)
- f) A polynomial f(x) has remainder 9 when divided by (x-3) and remainder -5 when divided by 2x+1. Find the remainder when divided by (x-3)(2x+1) (3 Marks)
- g) In an arithmetic progression the 4^{th} term is 13 and the 7^{th} term is 22. Find;
 - (i) The first term and the common difference

(2 Marks)

(ii) The value of n if the n^{th} term is 100

(2 Marks)

(iii) The value of m if the sum of m terms of the series is 175.

(3 Marks)

h) The roots of the equation $5x^2 + 12x + 6 = 0$ are α and β . Find the equation of the integral coefficients whose roots are $(\alpha - 1)$ and $(\beta - 1)$.

QUESTION TWO: (20 MARKS)
a) Simplify
$$\frac{\frac{1}{2}x^2(1+x)^{-\frac{1}{2}} - \frac{1}{2}x^{-\frac{1}{2}}(1+x)^{\frac{1}{2}}}{x}$$
 (4 Marks)

- Use Complete the square method to solve for x in the function $x^2 + x + 1 = 0$ (4 Marks)
- c) If $0 < x < \prod$ and tan(X A) = 3, where tan A = 2, show that $x = \frac{3}{4} \prod$ without using tables.

(4 Marks)

d) Find the first four terms in the expansion of $\sqrt{1-8x}$ in ascending power of x. Hence, substitute x=0.01and obtain the value of 23 correct to four significant figures (8 Marks)

QUESTION THREE: (20 MARKS)

a) Solve for
$$x$$
 given $log_2 1 + log_4 \frac{1}{2} = log_9 x$ (4 Marks)

b) Show that the solution of the general quadratic equation
$$ax^2 + bx + c = 0$$
 is given by

Hence solve the equation $x^2 + 15x + 56 = 0$.

(7 Marks)

- c) Find the general solution of the equation $\cos 2x 3\cos x + 2 = 0$ (7 Marks)
- d) State the quotient and the remainder when $9x^3 5x + 5$ is divided by 2x 5(2 Marks)

QUESTION FOUR: (20 MARKS)

- a) Show that $tan(A B) = \frac{\tan A \tan B}{1 + \tan A \tan B}$ (6 Marks)
- b) How many even numbers greater than 50000 can be formed using the digits 0,3,4,5,6,7
 - (i) without repetitions (6 Marks)
 - (ii) if repetitions are allowed (4 Marks)
- c) Simplify without using tables or calculator;

$$4\cos 30^{\circ} \sin 27.59^{\circ} - 4\sin 45^{\circ} \cos 62.41^{\circ} - 16\tan 45^{\circ} \sin 60^{\circ}$$
 (4 Marks)

QUESTION FIVE: (20 MARKS)

a) Simplify
$$\frac{\sqrt{xy} \times x^{\frac{1}{3}} \times 2y^{\frac{1}{4}}}{(x^{10}y^9)^{\frac{1}{12}}}$$
 (3 Marks)

- b) The first term of an arithmetic progression is -12, and the last term is 40. If the sum of the progression is 196, find the number of terms and the common difference. (5 Marks)
- c) Ksh. 100,000 was invested on 1st January 1990. An additional of Ksh. 6,000 was added to the investment at the beginning of each subsequent year. The investment earns a compound interest of 8% per annum. Find the value of the investment on 31st December 2000. (7 Marks)
- d) Find the first four terms in the expansion of $(1 8x)^{\frac{1}{3}}$ in ascending powers of x. Hence, substitute $x = \frac{1}{100}$ and obtain the value of $\sqrt[3]{23}$ correct to 5 significant figures (5 Marks)