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**KIRIRI WOMENS' UNIVERSITY OF SCIENCE AND TECHNOLOGY**  
**UNIVERSITY EXAMINATIONS, 2024/2025 ACADEMIC YEAR**  
**SECOND YEAR, SECOND SEMESTER EXAMINATION**  
**FOR THE DEGREE OF BACHELOR OF SCIENCE (COMPUTER SCIENCE)**

**KMA 2202: VECTOR ANALYSIS**

**DATE: 5<sup>TH</sup> DECEMBER, 2024**  
**TIME: 11:30AM-1:30PM**

**INSTRUCTIONS TO CANDIDATES**

**ANSWER QUESTION ONE (COMPULSORY) AND ANY OTHER TWO QUESTIONS**

**QUESTION ONE: COMPULSORY (30 MARKS)**

- (a) If  $A = i - j + 2k$ ,  $B = 2i - 3j + k$  and  $C = 3i - 2j + 2k$ , find  $(A \times B) \times C$ . (3 Marks)
- (b) Two sides of a triangle are formed by the vectors are  $A = 2i - 6j - 2k$  and  $B = 5i - j + 3k$  where the other side is obtained by finding the resultant of sides A and B. Determine the angles of the triangle. (5 Marks)
- (c) Find the area of a triangle having vertices at P (1, 3, 2), Q (2, -3, 1) and R (-1, 4, 3). (4 Marks)
- (d) The acceleration of a particle at any time  $t \geq 0$  is given by  $\frac{dv}{dt} = 12 \cos 2t i - 8 \sin 2t j + 16t k$ . If the velocity  $v$  and displacement  $r$  are zero at  $t=0$ . Find  $v$  and  $r$  at any time. (5 Marks)
- (f) Find the equation for the tangent plane to the surface  $2xz^2 - 3xy - 4x = 7$  at the point (1, -1, 2). (4 Marks)
- (g) Find a unit vector to any point in the curve  $x = a \cos \omega t$ ,  $y = a \sin \omega t$ ,  $z = bt$ , where  $a, b, \omega$  are constants. (4 Marks)
- (h) Evaluate  $\iiint_V (2x + y) dV$  where V is the closed region bounded by the cylinder  $z = 4 - x^2$  and the planes  $x = 0$ ,  $y = 0$ ,  $y = 2$  and  $z = 0$  (5 Marks)

**QUESTION TWO: (20 MARKS)**

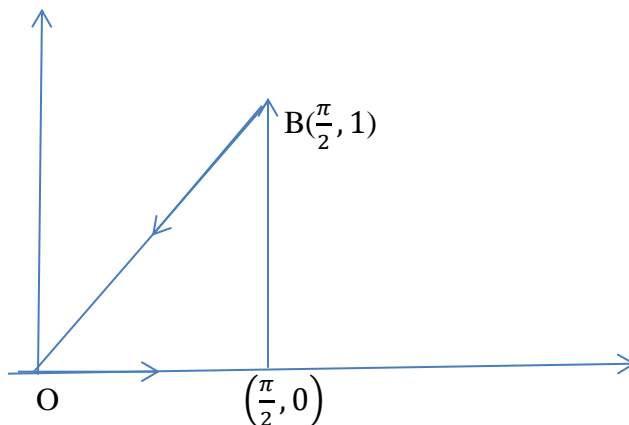
- (a) Find the work done in moving a particle in the force field  $F = 3xyi - 5zj + 10xk$  along the space curve  $x = t^2 + 1$ ,  $y = 2t^2$ ,  $z = t^3$  from  $t = 0$  to  $t = 2$ . (6 Marks)
- (b) If  $\frac{d^2A}{dx^2} = 6t i - 24 t^2 j + 4 \sin t k$ , find A given that  $A = 2i + j$  and  $\frac{dA}{dt} = -i - 3k$  at  $t = 0$ . (5 Marks)
- c) If  $\phi = 2xyz^2$ ,  $F = xyi - zj + x^2k$  and C is the curve  $x = t^2$ ,  $y = 2t$ ,  $z = t^3$  from  $t = 0$  to  $t = 1$ , evaluate the line integral;
- i.  $\int_C \phi dr$  (4 Marks)
- ii.  $\int_C F \times dr$  (5 Marks)

### **QUESTION THREE: (20 MARKS)**

- a) Find the angle between the surfaces  $x^2 + y^3 + z^2 = 9$  and  $z = x^2 + y^3 - 3$  at the point  $(2, -1, 2)$ . (5 Marks)
- b) Evaluate the line integral  $\int_C -4x dx + y^2 dy - yz dz$  with  $C$  given by  $x = -t^2$ ,  $y = t$ ,  $z = -3t$  for  $0 \leq t \leq 1$ . (5 Marks)
- c) Find an equation for the tangent plane to the surface  $xz^2 + x^2y = z - 1$  at the point  $(1, -3, 2)$ . (5 Marks)
- d) A particle moves along a curve whose parametric equations are  $x = 2 \sin 3t$ ,  $y = 2 \cos 3t$ ,  $z = 8t$ , where  $t$  is the time.
- i. Determine its velocity and acceleration at any time. (3 Marks)
- ii. Find the magnitudes of the velocity and acceleration. (2 Marks)

### **QUESTION FOUR: (20 MARKS)**

- (a) If  $A = yx^2 i - 2xz j + 2yz k$ , find  $\nabla^2 A$ . (5 Marks)
- (b) If  $A = (3x^4 + 6y)i - 14yz j + 20xz^3 k$ , evaluate  $\int_C A \cdot dr$  along the straight lines from  $(2, 1, 0)$  to  $(2, 1, 1)$ . (5 Marks)
- (c) If  $F = 3x^3 y i - y^2 j$ , evaluate  $\int_C F \cdot dr$  where  $C$  is the curve in the  $xy$ -plane,  $y = 2x^3$  from  $(0, 0)$  to  $(1, 2)$ . (3 Marks)
- (d) Verify Green's theorem in the plane for  $\oint_C (y - \sin x) dx + \cos x dy$ , where  $C$  is the triangle of the adjoining figure.



(7 Marks)

### **QUESTION FIVE: (20 MARKS)**

- (a) Prove that the vector  $A = 3y^4 z^2 i + 4x^3 z^2 j - 3x^2 y^2 k$ , is solenoidal. (5 Marks)
- (b) If  $F = (2x^2 - 3)i - 2xy j - 4x k$ , evaluate  $\iiint_V F \cdot dV$ , where  $V$  is the closed region bounded by the planes  $x = 0$ ,  $y = 0$ ,  $y = 6$ ,  $z = x^2$  and  $z = 4$ . (7 Marks)
- (c) If  $A = 2xz i - x j + y^2 k$ , evaluate  $\int_C A \cdot dr$  along the straight lines from  $(0, 0, 0)$  to  $(1, 1, 1)$ . (4 Marks)
- (d) Find a unit vector parallel to the resultant of the vectors  $r_1 = 2i + 4j - 5k$  and  $r_2 = i + 2j + 3k$  (4 Marks)