



Kasarani Campus
Off Thika Road
P. O. Box 49274, 00101
NAIROBI
Westlands Campus
Pamstech House
Woodvale Grove
Tel. 4442212
Fax: 4444175

KIRIRI WOMENS' UNIVERSITY OF SCIENCE AND TECHNOLOGY
UNIVERSITY EXAMINATIONS, 2024/2025 ACADEMIC YEAR
THIRD YEAR, SECOND SEMESTER EXAMINATION
FOR THE DEGREE OF BACHELOR OF SCIENCE (COMPUTER SCIENCE)

KCS 2308: FORMAL LANGUAGES AND AUTOMATA THEORY

DATE: 13TH DECEMBER, 2024
TIME: 11:30AM-1:30PM

INSTRUCTIONS TO CANDIDATES

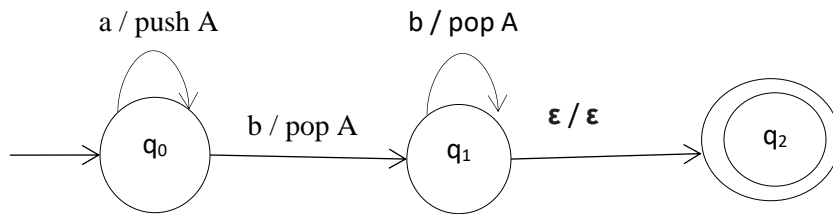
ANSWER QUESTION ONE (COMPULSORY) AND ANY OTHER TWO QUESTIONS

QUESTION ONE: COMPULSORY (30 MARKS)

- a) Given the alphabets $\Sigma_1 = \{0, 1\}$ and $\Sigma_2 = \{a, b, c\}$ Identify the concatenation $\Sigma_1 \Sigma_2$ (2 Marks)
- b) Distinguish between
 - i) terminal and non-terminal symbols (2 Marks)
 - ii) $X = \{a, b, c, d\}$ and $Y = \{1, 2, 3, 4, \dots\}$ (2 Marks)
 - iii) inductive and deductive proof (2 Marks)
 - iv) right linear grammar and left linear grammar (2 Marks)
 - v) 5^* and 5^+ (2 Marks)
- c) Determine $|S|$ if $S = \text{'cabcad'}$ (2 Marks)
- d) Describe (in English) the language defined by the following regular expression:
(letter | _) (letter | digit | _) * (2 Marks)
- e) Given the language $L = \{aaa, aab, aba, abb, baa, bab, bba, bbb\}$ determine its regular expression $L(r)$ (2 Marks)
- f) If $\Sigma = \{0, 1\}$, what is Σ^n when $n=4$ (2 Marks)
- g) With the aid of a diagram highlight the various types of grammars described in the Chomsky hierarchy (2 Marks)
- h) State how the output in a Mealy machine is affected by changes in input, as compared to a Moore machine (2 Marks)
- i) With reference to the Church-Turing thesis highlight whether artificial intelligence systems can ever surpass human reasoning (2 Marks)
- j) Explain how ambiguity affects the parsing of a language (2 Marks)
- k) With reference to the Halting Problem highlight whether artificial intelligence systems can be designed to solve every computational problem (2 Marks)

QUESTION TWO (20 MARKS)

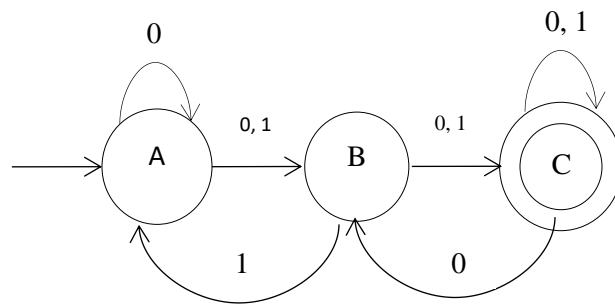
- a) Provide the formal representation of a push-down automata (PDA) (4 Marks)
- b) Explain the role of stacks within PDA (3 Marks)
- c) Highlight how PDAs are more powerful than FAs when it comes to language recognition (2 Marks)
- d) Given a context-free language $L = \{a^n b^n \mid n \geq 1\}$ provide a step by step description of how a PDA works to recognize the string "aabb" (6 Marks)



- e) Design a basic PDA for recognizing palindromes over the alphabet $\Sigma = \{a, b\}$ (5 Marks)

QUESTION THREE (20 MARKS)

- a) Design a finite automata (FA) for the following regular expression: $xy+(x+yy)y$ (5 Marks)
- b) Draw a deterministic finite automaton (DFA) that recognizes the language over the Alphabet $\Sigma = \{0, 1\}$ consisting of all those strings that contain an odd number of 1's (3 Marks)
- c) Provide the meaning of the following: $\delta(q_3, a) = \{q_0, q_1, \dots, q_n\}$ (2 Marks)
- d) Given the below NDFA. Provide its equivalent DFA using the subset construction method [show all steps used] (6 Marks)



- e) Highlight the basic limitation of a finite automata (2 Marks)
- f) Differentiate between regular and non-regular languages with reference to finite automata (2 Marks)

QUESTION FOUR (20 MARKS)

- a) Provide the formal representation of a context free grammar (CFG) (4 Marks)
- b) Given the language $L = \{a^n b^m \mid n \geq 0, n \leq m \leq 2n\}$ Generate the CFG for L (4 Marks)
- c) Given a string of the form $a+a^*a$. Let the set of production rules in a CFG over an alphabet $\Sigma = \{a\}$ be $X \rightarrow X+X \mid X^*X \mid X \mid a$
- Provide the leftmost derivation for the string (3 Marks)
 - Provide the rightmost derivation for the string (3 Marks)
 - Provide a unique set of productions for the string (3 Marks)
 - Provide the parse tree for the string using the unique set of productions obtained in (iii) above (3 Marks)

QUESTION FIVE (20 MARKS)

- a) Provide the formal representation of a Turing Machine (6 Marks)
- b) Design a Turing Machine for an equal number of a's and b's (4 Marks)
- c) Identify **TWO** extensions of Turing machines (2 Marks)
- d) Distinguish between unsolvable and undecidable problems with reference to Turing Machines (2 Marks)
- e) Provide the meaning of the following: $\delta(q_3, 1, R)$ (2 Marks)
- f) Outline **FOUR** basic features of Turing Machines that differentiate them from finite automata (4 Marks)